



“XFEM Analysis of Gas-Driven Crack Propagation Around a Blast Hole”

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One dimensional equations of gas flow

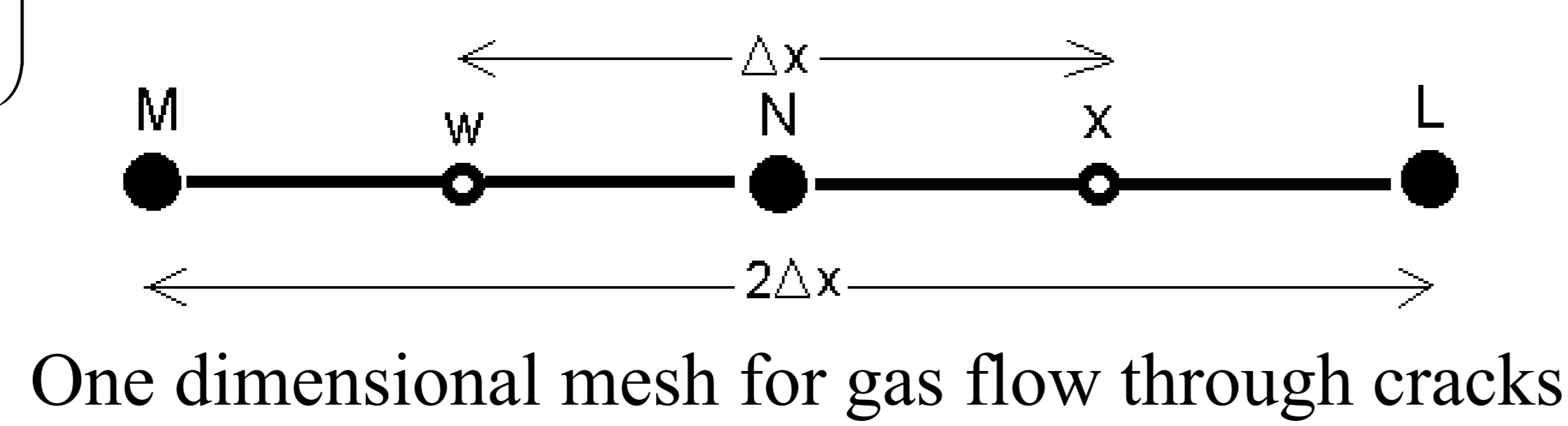
$$\frac{\partial(\rho h)}{\partial t} + \frac{\partial(\rho v h)}{\partial x} = 0$$

$$\frac{\partial(\rho v h)}{\partial t} + \frac{\partial(\rho v^2 h)}{\partial x} = -\rho h \left(\frac{1}{\rho} \frac{\partial P}{\partial x} + \psi \right)$$

$$\psi = \begin{cases} \frac{12 \mu v}{\rho h^2} \\ a \left(\frac{\varepsilon}{h} \right)^b \frac{v^2}{h} \end{cases}$$

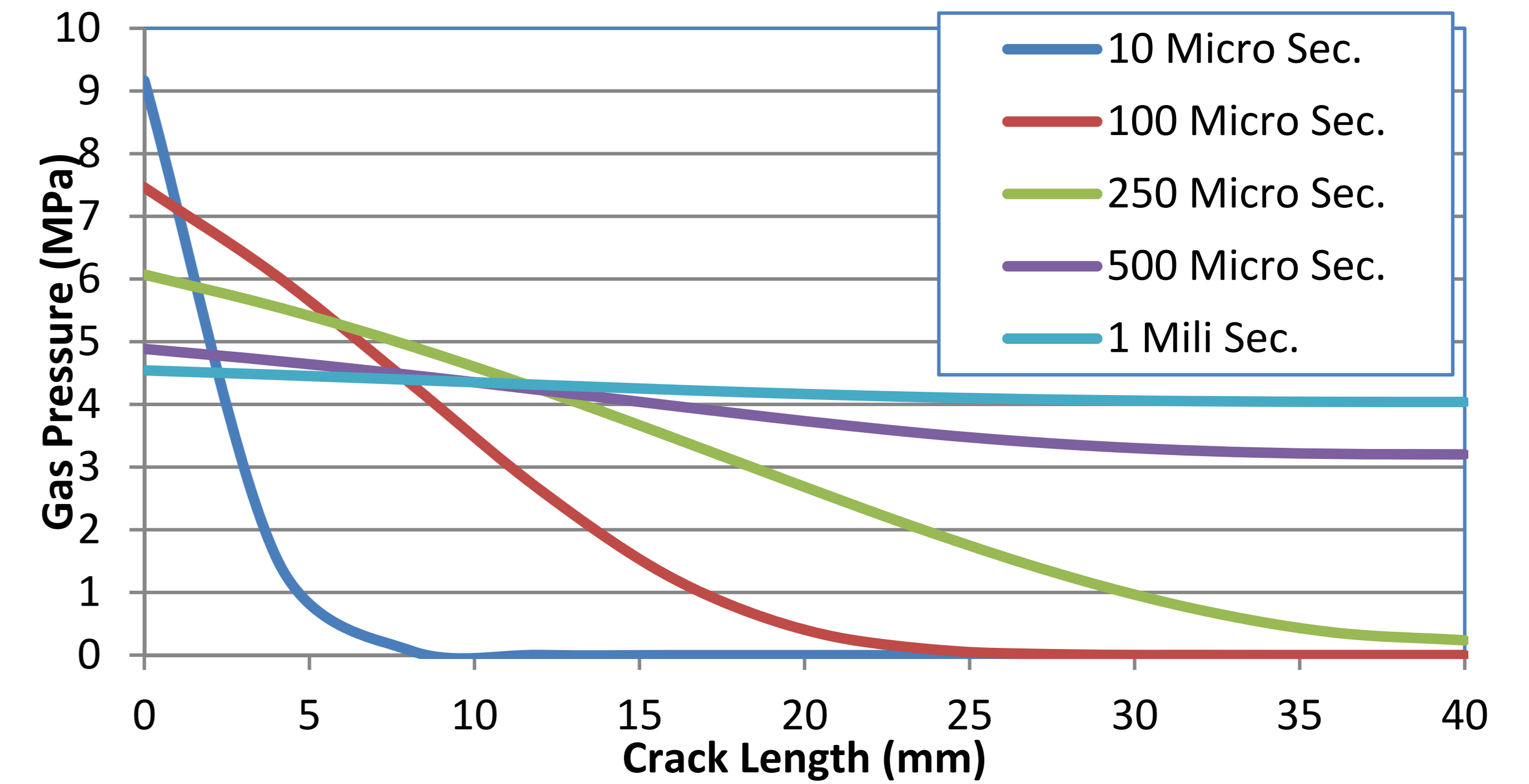
Equation of state

$$P = P_0 \left(\frac{\rho}{\rho_0} \right)^\gamma$$



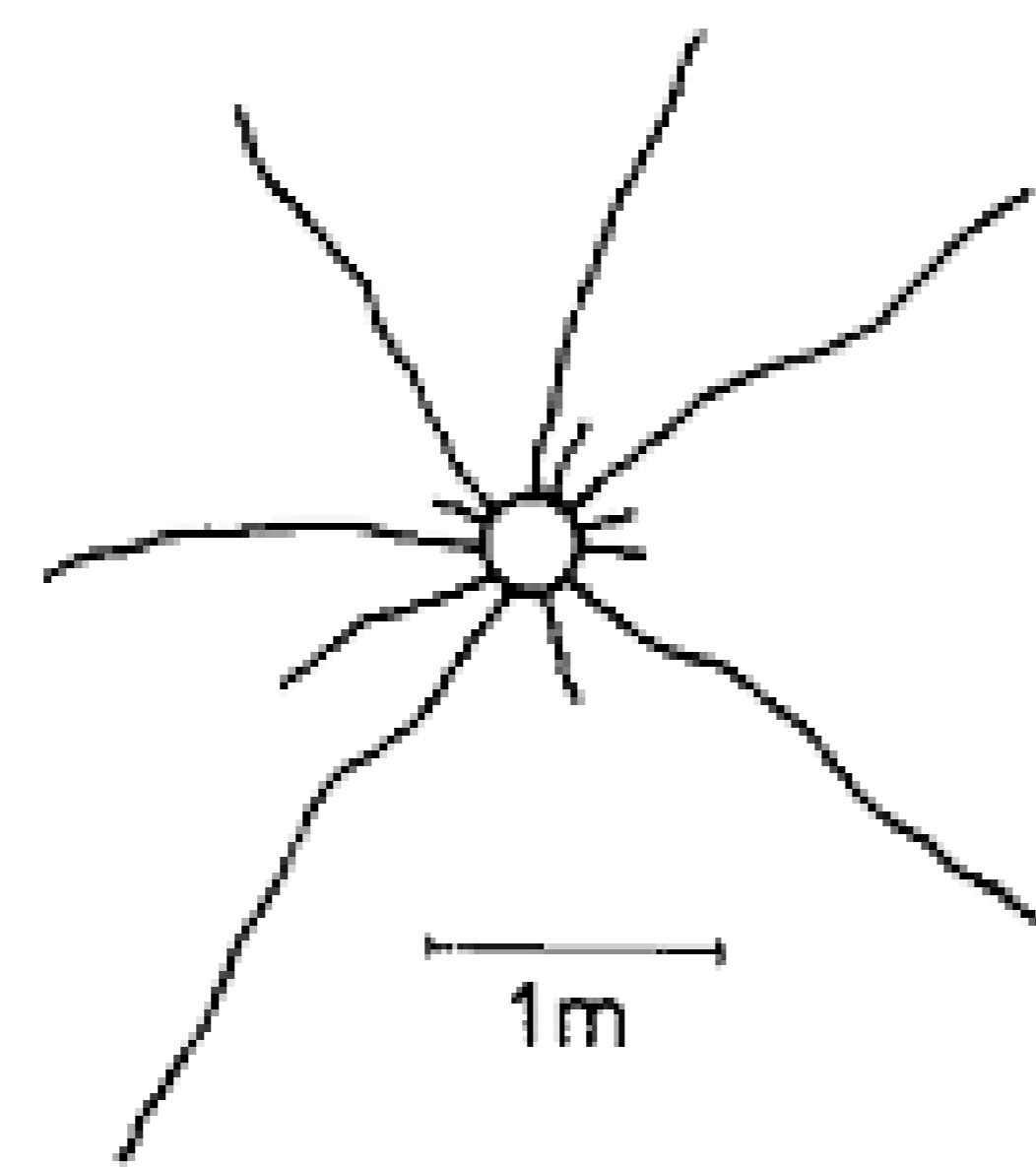
Gas pressure development through a crack, which is connected to a source of gas

$P_0 = 10 \text{ MPa}$
 $\rho_0 = 0.39 \text{ Kg/m}^3$
 Crack length = 40 cm
 $h = 2 \text{ mm}$
 $\varepsilon/h = 1$
 $\gamma = 1.29$

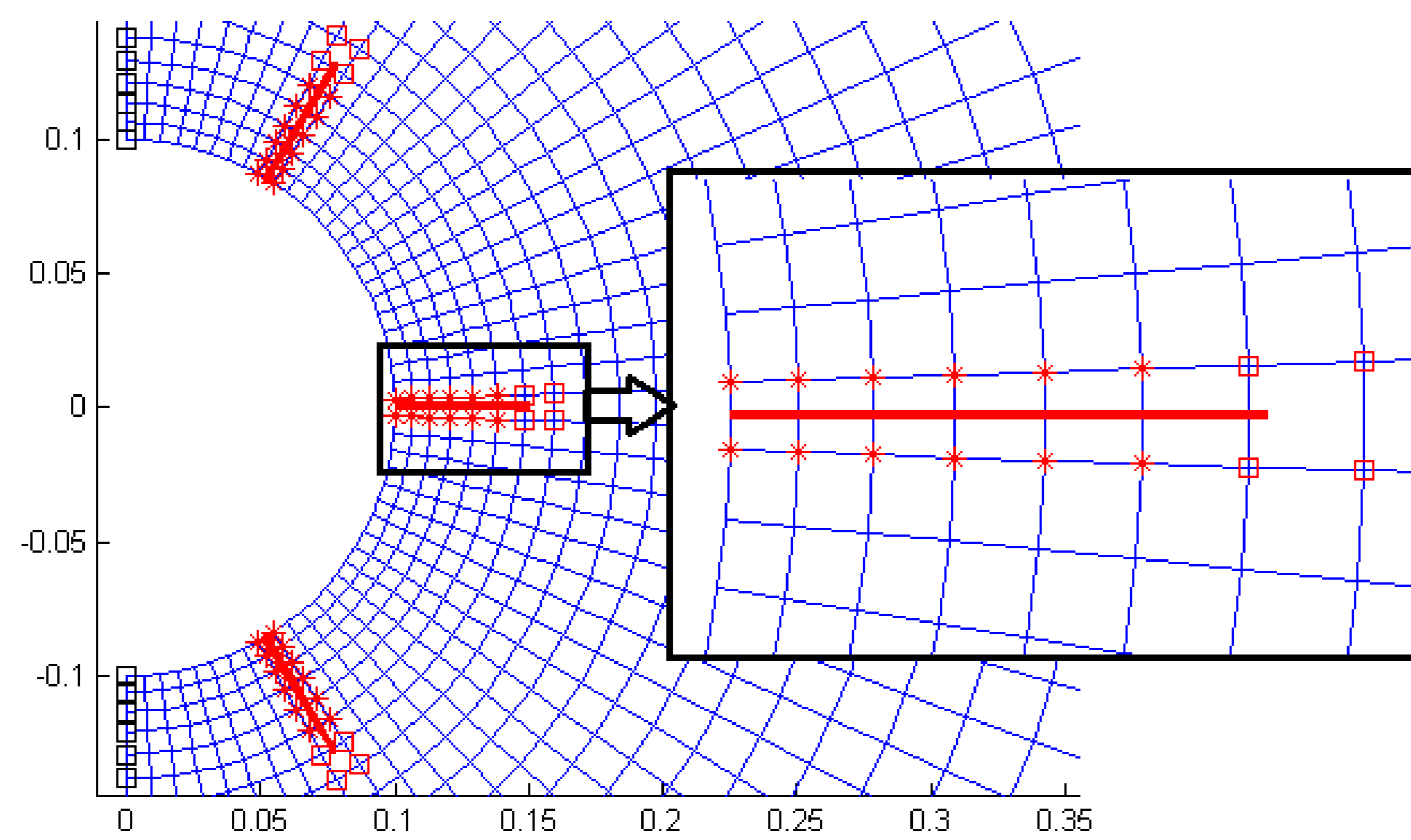
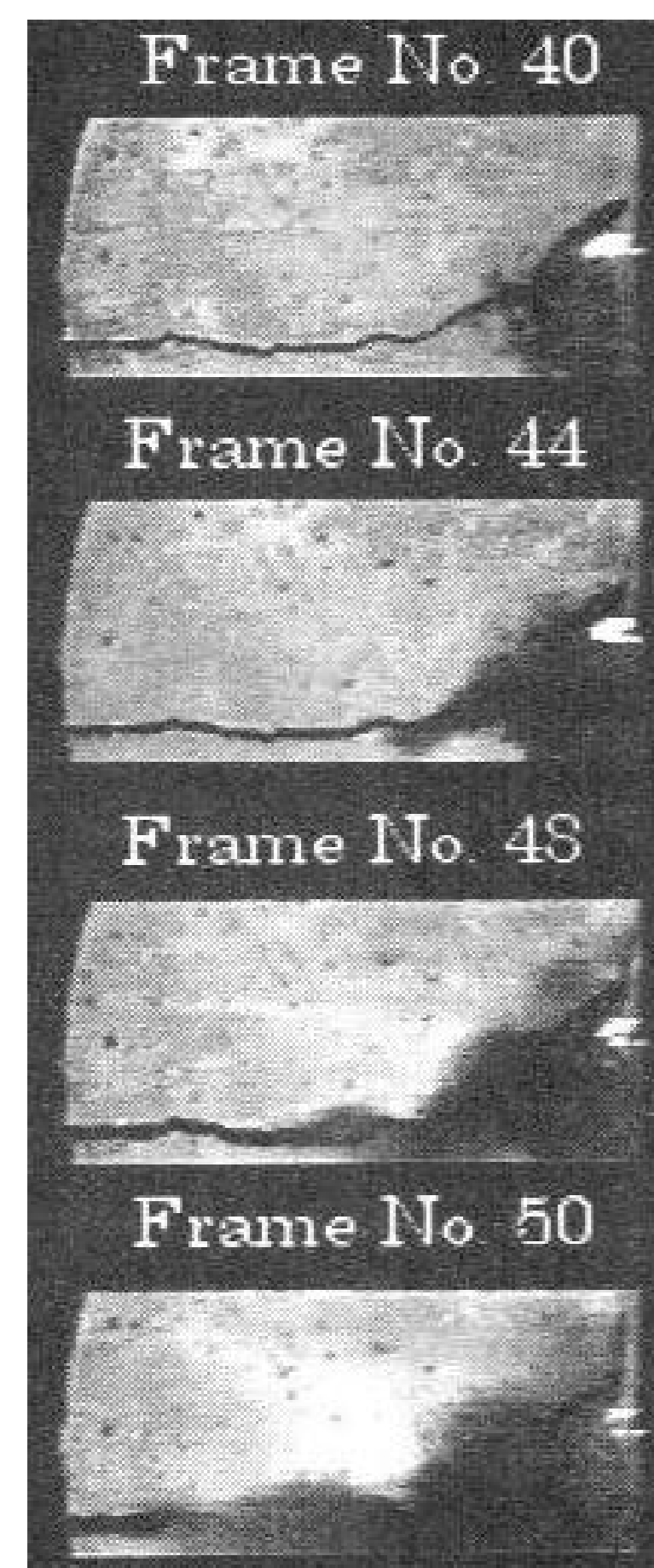


Sandia Lab Experiment

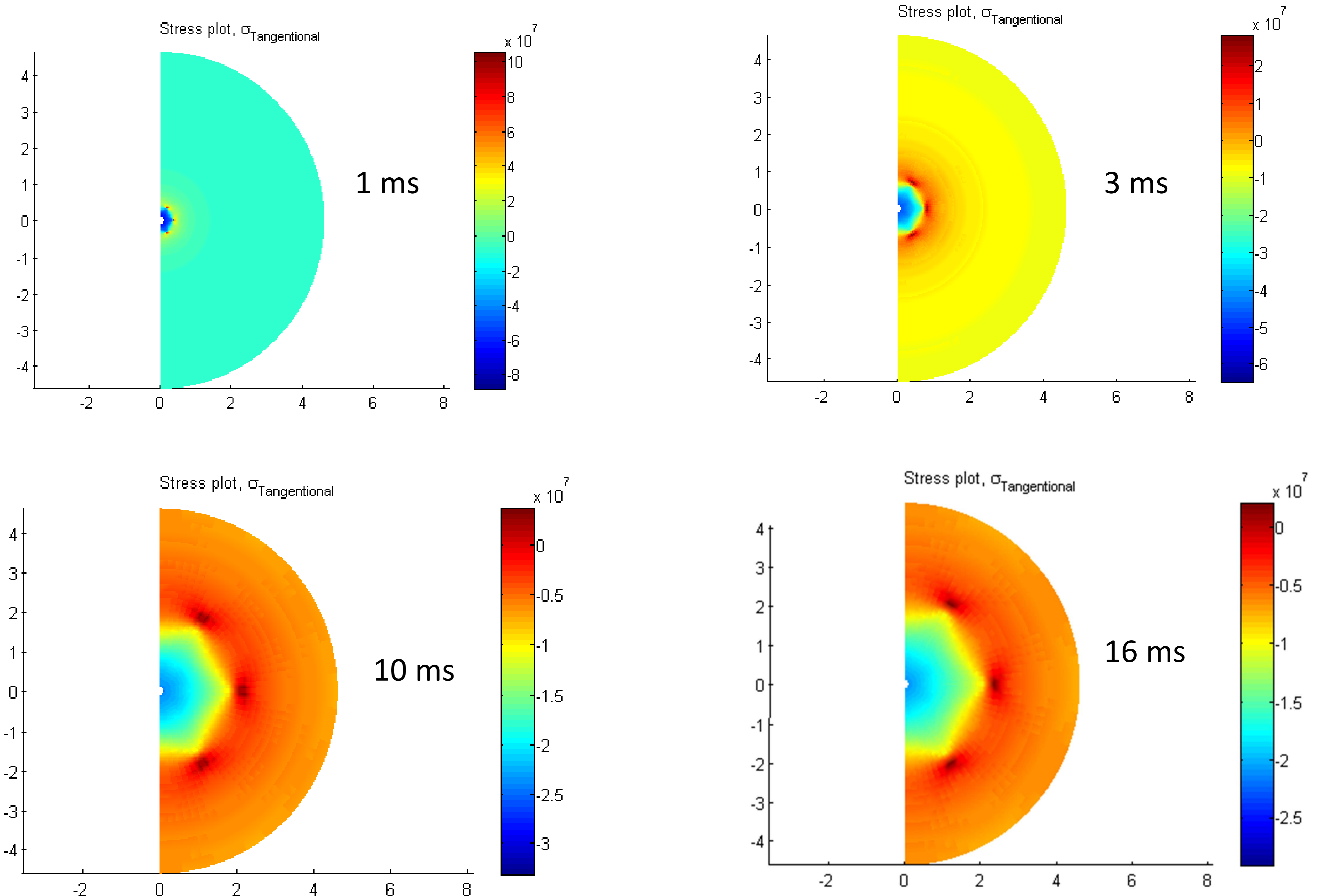
$P_0 = 90 \text{ Mpa}$
 Confining stress = 10 MPa
 Bore hole diameter: 0.2 m
 Charge diameter: 0.2 m
 Charge density: 0.5 gr/cm³
 Toughness = 0.5 Mpa/m^{0.5}
 $\gamma = 1.29$
 Number of cracks: 7
 Average Length: 1.7 m



Observed pattern of cracks



XFEM model



Crack propagation and stress contours