Analysis of transpression within contractual fault steps using finite-element method

Seyed Tohid Nabavi a,∗, Seyed Ahmad Alavi a, Soheil Mohammadi b, Mohammad Reza Ghassemi c, Marcel Frehner d

a Faculty of Earth Sciences, Department of Geology, Shahid Beheshti University, Tehran, Iran
b High Performance Computing Laboratory, School of Civil Engineering, University of Tehran, Tehran, Iran
c Research Institute for Earth Sciences, Geological Survey of Iran, Tehran, Iran
d Geological Institute, NO E3, ETH Zürich, Sonneggstrasse 5, Switzerland

A R T I C L E   I N F O

Article history:
Received 15 November 2016
Received in revised form 4 January 2017
Accepted 18 January 2017
Available online 21 January 2017

Keywords:
Transpression
Strike-slip fault
Fault segment
Contractional step
Finite-element method

A B S T R A C T

Two-dimensional finite-element modelling of elastic Newtonian rheology is used to compute stress distribution and strain localization patterns in a transpression zone between two pre-existing right-stepping, left-lateral strike-slip fault segments. Three representative fault segment interactions are modelled: underlapping, neutral, and overlapping. The numerical results indicate that at the onset of deformation, displacement vectors are oblique to the regional compression direction (20°–90°). The orientations of the local σ1 (the maximum compressive stress) and σ3 (the minimum compressive stress) directions strongly depend on the structural position within the transpression zone. For neutral and overlapping fault steps, there is a contractual linking damage zone between the fault segments. For overlapping faults, the σ1 trajectories within the transpression zone deflect significantly forming a sigmoidal pattern, which is created by two rotational flow patterns close to the fault tips. These flow patterns are related to friction effects and different shear deformation, from pure shear outside of the fault steps toward simple shear along the fault segments. Interaction between the two fault segments perturbs the stress field and reflects the heterogeneous nature of deformation. A lozenge- (for underlapping steps), rhomboidal- (for neutral steps), and sigmoidal-shaped (for overlapping steps) transpression zone developed between the two segments. The modelled mean stress pattern shows a similar pattern to that of the contractional steps, and decrease and increase in underlapping and overlapping fault steps, respectively. Comparison of the Kuh-e-Hori transpression zone, between the Esmail-abad and West Neh left-stepping right-lateral strike-slip fault segments in SE Iran, with the modelling results shows strong similarities with the neutral step configuration.

© 2017 Elsevier Ltd. All rights reserved.

1. Introduction

On geological maps, strike-slip fault systems are often apparently linear and relatively continuous (Dasgupta and Mukherjee, 2016). However, in nature they are typically discontinuous and segmented on various scales. Such sub-parallel discontinuous fault segments often exhibit en-échelon, non-coplanar geometries and include steps and bends in the master fault that demarcate the boundaries of the strike-slip zones. The individual fault segments are separated from each other and interact through their stress/strain fields. The movement on the fault segment parallel each other and initiates shear fracture/fault (Segall and Pollard, 1983; Pollard and Segall, 1987; Aydin et al., 2006). The represent step-overs between two fault segments represent the locations of extensional or contractual heterogeneous deformations depending on the sense of fault step with respect to the sense of slip along the main strike-slip fault system (Fig. 1). The sense of step is described as left- and right-stepping. Releasing or extensional stepovers result where the sense of step is the same as the sense of the overall slip (e.g., a left-step along a left-lateral fault) (Biddle and Christie-Blick, 1985; Christie-Blick and Biddle, 1985; Woodcock and Fischer, 1986; Sylvester, 1988; Woodcock and Schubert, 1994; Westaway, 1995; Cunningham and Mann, 2007; Mann, 2007; Crider, 2015; Cao and Neubauer, 2016; Kattenhorn et al., 2016;
related structures include open and dilatant cracks at cm to m-scale (e.g., Segall and Pollard, 1980, 1983; Martel et al., 1988; Kim et al., 2000, 2003, 2004; Flodin and Aydin, 2004) and pull-apart basins, sag ponds and negative flower structures (e.g., Mann et al., 1983; Aydin and Nur, 1985; Mukherjee, 2015a, 2015b). However, all these structures need not form in every strike-slip settings (Misra et al., 2014, 2015, 2016; Misra and Mukherjee, 2015, in press-1, in press-2; Babar et al., in press; Kaplay et al., in press, submitted; Mukherjee et al., in press). In contrast, restraining or contractual stepovers, or contractual linking damage zone (Kim et al., 2004), result where the sense of step is opposite to the sense of the overall slip (e.g., a right-step along a left-lateral fault or vice versa) (Biddle and Christie-Blick, 1985; Christie-Blick and Biddle, 1985; Woodcock and Fischer, 1986; Sylvester, 1988; Woodcock and Schubert, 1994; Westaway, 1995; Cunningham and Mann, 2007; Mann, 2007; Crider, 2015; Kattenhorn et al., 2016; Peacock et al., 2016); related structures include closing, anti-cracks and pressure solution seams at the m-scale (e.g., Bürgmann and Pollard, 1992, 1994; Peacock and Sanderson, 1995) and pop-up and positive flower structures at the regional scale (e.g., Aydin and Nur, 1985). Contractual fault steps, which are common features of active intra-continental strike-slip fault systems, are commonly referred to as sites of “transpression” (e.g., Curtis, 1997, 1999; McClay and Bonora, 2001; Dooley and Schreurs, 2012). Depending on the assumed fault plane orientation, the extensional and contractual steps may be classified as either “transpression” (Fig. 1a) or “transpression” (Fig. 1b), respectively (Fig. 1). Transpression results in a combination of simple- and pure-shear components (Sanderson and Marchini, 1984; Fossen and Tikoff, 1993, 1998; Fossen et al., 1994; Mukherjee and Koyi, 2010a; Fossen et al., 2013) and related structures (Mukherjee, 2010a, 2013a, 2013b, 2015a, 2015b) on the wide variety of scales from lithospheric plate downwards in any strike-slip zone that is not perfectly planar. Hence transpression zones (non-Andersonian case) can be related to the boundary conditions and obliquity between the imposed compressive stress and plate boundaries (Upton and Koons, 2007; Mukherjee and Koyi, 2010b; Mukherjee, 2012a, 2012b; Fernández et al., 2013; Díaz-Azpiroz et al., 2014; Mukherjee, 2014a, 2014b; Mukherjee and Biswas, 2014, 2015; Díaz-Azpiroz et al., 2016; Frehner, 2016a, 2016b; Nabavi et al., 2016a, 2016b; Philippon and Corti, 2016; Zanchi et al., 2016).

Real geometries of contractual strike-slip fault steps, however, vary more due to the initial separation and increasing offset of faults segments (e.g., Rodgers, 1980; Mann et al., 1983). Numerous field studies (Bürgmann and Pollard, 1994 as for example), analytical studies (Pollard and Segall, 1987 as for example), analog modelling studies (McClay and Bonora, 2001; Dooley and Schreurs, 2012; Gonzalez et al., 2012; Cooke et al., 2013; Barcos et al., 2016), and simulations (Willemse et al., 1996; Li et al., 2009; Strijker et al., 2013; Dasgupta et al., 2015; Nevitt, 2015, Frehner, 2016a, 2016b) investigated the behavior of transpression within contractual fault steps and the mechanical interaction between nearby fractures/faults. Mechanical modelling of a fault step avoids many of common assumptions, for example homogeneous deformation, inherent to kinematic models (Nevitt et al., 2014; Nevitt, 2015). These studies identified certain basic variables that influence the evolution of transpressional deformation in contractual fault steps, such as the fault overlap-to-separation ratio and the relative orientation of faults. The mechanical interaction between fault segments helps rationalize the overlap-to-separation ratio, their hook-shaped geometry (different from “hook fabric”: Mukherjee and Koyi, 2010b), why some fractures/faults selectively terminate, whereas others propagate, and also deviates systematically from simple systematic slip distributions (Pollard and Aydin, 1988; Willemse et al., 1996; Lunn et al., 2008; Strijker et al., 2013; Lejri, 2015; Lejri et al., 2015). Static sliding friction coefficient strongly affects the fault mechanical properties and local stress field (Willemse and Pollard, 1998; Mutlu and Pollard, 2008; Maerten, 2010; Soliva et al., 2010; Ritze et al., 2015; Maerten et al., 2016; Mukherjee, 2017).

Numerical techniques, especially the finite-element (FE) method, are powerful to provide comprehensive insight beyond the direct observations, such as the stress state, strain and deformation patterns during and after the structural evolution. For example, Gölte et al. (1994) analyzed the vertical displacement, topographic variation, and pull-apart basin formation as a function of the relationship between fault geometries (underlap, neutral, and overlap states) in the releasing stepover along left-stepping left-lateral strike-slip faults using two-dimensional elastic FE-models. They showed two sub-basins separated by a broad zone of relative uplift forming in fault underlap. Bertoluzza and Perotti (1997) used a series of frictionless FE fault models to simulate the stress filed associated with pure strike-slip, transtensional, and transpressional conditions. They showed that the angle between the potential normal faults and the strike-slip faults strongly depended on the overall boundary conditions and only slightly on the rheological properties and the overlap-to-separation ratio of the faults. In addition, Misra et al. (2009) showed that reactivation of pre-existing fractures in presence of compressional shear loading conditions usually involved frictional sliding along the fracture wall which could produce local tensile stress concentrations that can cause the propagation of horsttail (Granier, 1985), splay (Martel, 1990), and tail or wing faults (Willemse et al., 1997; Blenkinsop, 2000). Nevitt et al. (2014) and Nevitt (2015) studied a mechanical model of transpression within contractual planar overlapping faults in elastoplastic material using 2D plane-strain FE-modelling. In their model, the distribution of the minimum and maximum principal stretches deform locally in the step, so that no significant stretch (=final length/initial length) was deserved across the fault traces outside the step. As a result, the stretch ellipsoid varied in orientation throughout the step indicating...
heterogeneous deformation. However, the problem of stress distribution, strain localization, and transpression zone pattern in various convergence angles and geometries of frictional fault segments, parameters which strongly control the evolution of transpression zones within contractual fault step, has been less considered and compared with results of experimental modelling in these studies. Here the results of a systematic series of transpression zones are presented and compared with a range of natural, numerical, and experimental examples. It is of critical importance since deformation localizes around fault segment tips, the interaction between faults (as transpression boundaries) in different step geometries (such as underlap, neutral, and overlap configuration) is therefore expected to be significant. On the other words, knowledge of these problems using numerical and experimental models would be useful in interpreting transpression zones in areas of incomplete data.

We use a series of 2D FE-models through ABAQUS™ software package to simulate stress and strain features recorded in a transpression zone within the straight and parallel contractual fault step along a strike-slip fault system. We simulate the entire range of various tectonic regimes (i.e., pure strike-slip, transpression, pure contraction) by varying the convergence angles (0°, 30°, 45°, 60°, and 90°) and analyze the stress/strain fields by applying different sets of boundary conditions. The purposes of this study are 1) to understand the role of strike-slip fault separation and amount of overlap on the development and evolution of transpression zones, 2) to predict the possible fault pattern inside the transpression zone, 3) stress distribution and strain localization patterns and validated and compared with analogue and numerical experiments performed by other authors, and 4) to simulate various fault step geometries in natural examples.

Several types of boundary conditions (velocity, displacement, etc.), loadings (pressure, gravity, etc.), and contact formulations (surface to surface, general contact, node to surface, etc.) can be applied. Stress, strain, displacement and energy are among several output fields by applying different sets of boundary conditions. The purposes of this study are 1) to understand the role of strike-slip fault separation and amount of overlap on the development and evolution of transpression zones, 2) to predict the possible fault pattern inside the transpression zone, 3) stress distribution and strain localization patterns and validated and compared with analogue and numerical experiments performed by other authors, and 4) to simulate various fault step geometries in natural examples.

2. Finite element method

ABAQUS™ (ABAQUS/CAE), FE commercial program (ABAQUS™ tutorial version 6.14—2, 2014; www.simulia.com/) allows various element types and includes modules for several rheologies properties such as elasticity, plasticity (Mohr-Coulomb, Drucker-Prager, etc.), viscosity (linear, power law, etc.), and combinations thereof. Several types of boundary conditions (velocity, displacement, etc.), loadings (pressure, gravity, etc.), and contact formulations (surface to surface, general contact, node to surface, etc.) can be applied. Stress, strain, displacement and energy are among several output possibilities.

2.1. Model set-up

2D plain strain and linear elastic solid behavior (linear relation between stress and strain) is adopted for FE-modelling of transpression. The focus is on the interactions between two parallel, planar right-stepping left-lateral/sinistral strike-slip faults with equal lengths (a restraining step) that obey the Coulomb criterion for fault slip (Fig. 2a). Friction along the fault segments is constrained by a coefficient of 0.3—0.6 (Byerlee, 1978). In the present study it is 0.51 for sandstones (Pollard and Fletcher, 2005). Sliding occurs if traction on the fault exceeds 0.51 of the normal stress (Byerlee, 1978). The pair of fault segments strike obliquely to the direction of compressive normal stress applied to the model boundaries. The fault segments have a left-oblique component (Crider, 2001) that creates left-lateral movement/offset/slip. Surrounding the faults, we assume an isotropic homogenous linear elastic shell. Such an assumption was also made in similar studies by Goteti (2009), Strijker et al. (2013), Nevitt et al. (2014) and Nevitt (2015). Thus, the model presented in this work may not work for foliated rocks or for layered rock sequences. One reason for studying the elastic behavior is that the upper part of the lithosphere is often approximated as an elastic material (Turcotte and Schubert, 2014). Studies indicate that the rheology of the upper crust is elastic-plastic. Nevertheless, because the rheology is approximate, we use the elastic models to only investigate spatial patterns and relative amplitudes of deformation. Our analysis is thus a linear approximation to a non-linear process. Therefore, we do not attempt to predict absolute uplift, subsidence, or slip along faults but only a relative pattern of deformation. The 2D FE-model considers plane strain, which is valid if the faults are much longer in the Z-direction than in the X- and Y-directions. The effects of topography and crust curvature are ignored. To avoid the effects of model boundary on stress distribution, the model dimensions are

Fig. 2. a The general model set-up with two fault segments and boundary conditions. The finite element shown in (b) with decrease in size of element from the model edges towards the fault segments. The faults are pre-defined to strike at α = 0, 30, 45, 60 and 90° in a clock-wise sense from the Y-axis, where α is the convergence angle.
significantly larger (≥5 times) than the dimensions of the fault system (Misra et al., 2009), so that the applied boundary conditions simulate a far-field stress. A total of 23819 quad-dominant isotropic brick elements (23834 nodes) and two master left-lateral strike-slip faults describe a model of 80 × 80 km. Each fault segment is 10 km long. The size of elements decreases from the boundaries towards the faults to ensure sufficient accuracy whilst limiting computation time (Fig. 2b).

The used elastic parameters are as follows: Young’s modulus (E) 22 GPa and Poisson’s ratio (ν) 0.24 (based on Pollard and Fletcher, 2005; Jaeger et al., 2007) (Table 1). The elastic modelling parameters are kept constant for all experiments at physically realistic material property mean values representative for sandstones (Pollard and Fletcher, 2005; Jaeger et al., 2007). Previous numerical studies have shown that changing the elastic parameters does not produce significant changes in the modelling results (Gölke et al., 1994; Bertoluzza and Perotti, 1997; Bourne and Willemsen, 2001). A compressive normal stress is applied to two adjacent boundaries of the model with a maximum value of 80 MPa based on Strijker et al. (2013). In addition, a displacement boundary condition is introduced on the right model boundary that produces a bulk shortening of 3% across the model. Lower and left boundaries of the model are constrained by the condition that uy = 0 and ux = 0, to prevent rigid body rotation and translation during loading (Nevitt et al., 2014; Nevitt, 2015) (Fig. 2a). These boundary conditions define shear planes both parallel to the fault steps and parallel to internal faults (Westaway, 1995), which obliquely connect fault steps.

2.2. Modelling strategy

We use a right-stepping configuration of two left-lateral faults to quantify the effect of different step geometries on the stress and strain distribution throughout the model. The faults are pre-defined to strike at α = 0, 30, 45, 60 and 90 in a clock-wise sense from the Y-axis, where α is the convergence angle (assuming that modelling was monitored through a top-view) (Fig. 2a). The main parameters investigated in the current model series are the convergence angle, the angle of offset between the master fault segments (Leever et al., 2011; Dooley and Schreurs, 2012), and the step geometries. In present study, transpression is considered in different overlap-to-separation situations such as underlap, neutral, and overlap. Growth of the pre-defined faults is not considered, instead the focus is on the resulting stress and strain distribution as indicators for the potential development of subsequent fractures/faults. Overlap (O) and underlap (U) are measured from fault tip to fault tip, parallel to the main fault strike. Separation (S) is measured orthogonal to the main fault strike (Dooley and McClay, 1997; Dooley et al., 1999; McClay and Bonora, 2001; Long and Imber, 2011; Dooley and Schreurs, 2012; Corti and Dooley, 2015). S is 12.5% of the length of the fault segments (i.e. 1.25 km). Underlap and overlap are 25% of the length of the fault segments (i.e. 2.5 km). In addition, the step geometries are at 26° in case of underlapping step, 90° for neutral step, and 154° for the overlapping step (Fig. 3). These angles are measured between the strike of the main fault segments and the line joining the tips of the faults in the step zone. All other parameters, including the separation between the master fault segments and the initial width of the offset area/weak zone (i.e. overlap and underlap size) are kept constant.

3. Results

With increasing obliquity, various displacements on the adjacent strike-slip fault segments and within the fault step result in a wrapped (non-linear) displacement pattern in the transpression zone but systematic paths (with a specific pattern and angle relative to the fault segments and far-field stress). The deformed geometry and stress and strain contours clearly show – strike-parallel contraction along the faults. Opposing slip along the fault segments within transpression zone warps and tilts the model transpression zone, resulting in a combination of simple and pure shear (i.e. general shear/sub-simple shear). The displacement vectors are 20–45° oblique to the regional applied shortening direction. Contraction localization along the transpression zone boundaries compared to no significant contraction/stretch immediately across the fault segments (the outer parts of the zone) and ensures that displacements remain oblique to the regional transport direction throughout the deformation. Within the transpression zone the interaction of stress fields near the tip of the faults produces a complex stress field. Outside the transpression zone, the maximum compressive stress (σ3) orients sub-parallel to the applied regional compressive stress direction. Orientations of σ3 (the minimum compressive stress) and σ1 strongly depend on the structural position within the transpression zone. For underlapping fault steps, the highest rotation of these stresses is observed near the fault tips.

![Fig. 3. Separation and angular relationships of the steps for the three models presented in this study (after Dooley and McClay, 1997; Dooley et al., 1999; Dooley and Schreurs, 2012; Corti and Dooley, 2015): 26° underlapping, 90° neutral and 154° overlapping steps. The angles of the steps are identical in numerical models. Separation (S) is 12.5% of the length of the fault segments. Overlap (O) and underlap (U) is 25% of the length of the fault segments. Underlap and overlap are measured from fault tip to fault tip, parallel to the master fault strike. Separation is measured orthogonal to the master fault trend.](image-url)
(20°–70° relative to the fault segments), so that rotation decreases towards the central portion of the zone (almost parallel to the fault segments) (Fig. 4). For overlapping fault steps, $\sigma_1$ trajectories within the transpression zone are highly deflected, almost perpendicular to the applied stress orientation, which indicate a sigmoidal pattern (Fig. 5). $\sigma_1$ progressively rotates towards parallelism with the boundary faults as the convergence angle increases (from 30° to 60°). This sigmoidal pattern is created by two clockwise flow rotations around the fault tips due to friction effect and different shear component, from pure shear outside the fault steps towards simple shear along the fault segments. In a model with frictionless faults subjected to a remote shear stress parallel to the fault surfaces, the distribution of stress (Mises equivalent) and strain for contractional and extensional fault steps are mirror images of each other. Introducing friction and the contact properties necessary to prevent interpenetration impacts the two step geometries in distinct ways. This rotation of stress/strain vectors is higher than (10°–20°) in the case of neutral fault steps (Fig. 6). The rotation of stress orientations from the regional transport direction increases with increasing overlap-to-separation ratio.

For neutral and overlapping fault step configurations, the compressional quadrants (the maximum principal stress) of the inner fault tips are located inside the transpression zone (Figs. 5 and 6). This condition results in a relatively high $\sigma_3$ in this part. Low-$\sigma_3$ zones develop in and near all fault tips and are located outside the fault segments (Fig. 7). In low-$\sigma_3$ zones (high stretch) wing cracks and horsetail arrays would therefore develop outwards along a curvilinear path, aligned with the local $\sigma_1$ trajectories (Fig. 8). A contractual linking damage zone, generally with shear fractures (mode II and III), multiple fault sets, and non-coaxial displacements (Segall and Pollard, 1980; Kim et al., 2000, 2001, 2004; Jones et al., 2004; Goteti, 2009; Goteti and Mitra, 2013, 2016; Choi et al., 2016) are created between the neutral and overlapping fault steps. Therefore that the strain magnitude reduce laterally from the central portion of the transpression zone towards the tips of the fault segments. $\sigma_1$ and the maximum principal strain trajectories show a sigmoidal shape and progressive rotation, implying a distributed simple and pure shear within the transpression zone (Fig. 8). The rhomboidal (for neutral steps) and sigmoidal (for overlapping steps) transpressional zones (or pop-up structure) may be bounded by listric, oblique-slip reverse faults. This distributed stress/strain trajectories cause block rotation.

Two main types of fault interaction occur (Aydin and Schultz, 1990; Gupta and Scholz, 1998, 2000; Fossen and Rotevatn, 2016): 1) “hard-linkage”: faults occurs where faults directly, or through a transfer/accommodation zone link together and 2) “soft-linkage”: faults interact when faults interact only through their stress fields and the associated strained zone is without crosscutting faults. Underlapping fault steps for $\alpha = 0°–90°$, exhibit a well-developed $\sigma_3$ zone, roughly perpendicular to the fault segments that are linked together with a slightly oblique and a strong localization $\sigma_3$ zone within the transpression zone. The linkage zone of $\sigma_1$ trajectories

---

**Fig. 4.** Maximum principal strain distribution for underlapping steps under convergence angle of a) 0°; b) 30°; c) 45°; d) 60°; and e) 90°.
does not develop for $\alpha = 0^\circ-90^\circ$, where $\sigma_3$ zone localize in the tensional quadrant near the fault tips and $\sigma_3$ is actually relatively high in the central interaction zone of the fault segments. In all underlapping models, the lozenge-shape (Mukherjee, 2016) transpression zone are bounded by two dextral reverse faults. Differences between neutral and underlapping steps include higher stress concentration, increasing rotation, and the development of secondary shear displacement and structures in central portions of the zone due to the increasing amount of overlap. Stress concentration within transpression zones can exhibit uplift in 3-D models. In addition, overlapping steps display similar characteristics to the neutral steps, but develop a strong sigmoidal pop-up structure, bounded by curved, oblique slip reverse faults, and also increased rotation of stress trajectories in tips zone. These results resemble models of Dooley et al. (1999), McClay and Bonora (2001), and Dooley and Schreurs (2012).

In all present models, strain and stress trajectories rotation and variation in stress and strain magnitudes reflects a heterogeneous deformation, which ranges from approximately simple shear up to non-coaxial flattening strain. In other words, strain localization occurs in all models. In addition, the stretch ellipsoid (the amount of strain components after mapping all of them) varies in orientation across the step and constrain the heterogeneous deformation (e.g., Goteti, 2009; Goteti and Mitra, 2013, 2016). Increased friction along the faults tends to reduce the magnitude of the mean stress in the fault steps, as well as the size and extent of the region with the largest stress change (e.g., Kattenhorn and Pollard, 1999; Brankman and Aydin, 2004; Lejri, 2015; Lejri et al., 2015). The mean stress effectively shows uplift (contraction) and subsidence (extension) associated with faulting (Aydin and Schultz, 1990). In the overlapping fault steps with friction 0.51 and for all convergence angles, model results show low mean stresses to localize at fault tips and increasing mean stress towards the central portions of the zone as the two segments interact (Fig. 11). In neutral configurations, mean stresses localize more at fault tips than at the overlapping steps (Fig. 10). In contrast, for underlapping fault steps for all convergence angles, there is a concentrated low mean stresses between the segments (Fig. 9). The magnitudes of mean and shear stresses decrease and increase, respectively, from underlapping configuration toward overlapping fault steps, which is a consequence of the opposed relative motions of the two fault segments (Figs. 9–11) (e.g., Bürgmann and Pollard, 1992, 1994; Nemčok et al., 2002; Favreau and Wolf, 2009; Ritz, 2013; Ritz et al., 2015). Faults in brittle materials develop into the regions of lower mean stresses. Expectedly, results show that secondary faults develop away from one another (e.g. Segall and Pollard, 1980; Bürgmann and Pollard, 1994). Elastic models show that the mean stress, except for underlapping configurations, for all convergence angles is more compressive within the transpression zone than the region immediately outside the step and fault segment tips under tension. In all fault step models and convergence angles, except for $\alpha = 90^\circ$, $S_1$ (the maximum stretch) trajectories make a high angles (45–90°)
with the main fault segments. The angle between extensional structures, such as normal faults (parallel to the local trajectories), and the main strike-slip fault segments (clockwise from the fault segment) in the ranges $65^\circ - 100^\circ$. The results suggest that even when the major faults are compressed orthogonally and the overall deformation is plane strain, transpression zones can be involved by a complex three dimensional stress/strain field inconsistent with the regional strain field.

The Von Mises equivalent stress, which is a function of the principal stress difference and the maximum shear stress, in the transpression zone evolves into a stress field that differs from the far-field stresses outside the zone. This modification of stress field is more prominent in the case of overlapping steps than the neutral and underlapping steps. In almost all configurations, lobes of enhanced Von Mises equivalent stress extend beyond the fault tips and slightly beyond the fault segments (Figs. 12–14). In general, neutral and underlapping fault steps result in higher distortional stresses/strains at fault tips and in the central contractional area than in the case of overlapping faults, characterized by higher Von Mises stress in the transpression zone. This is because, distortion of the contractional zone accommodates most of the extension. Depending on the proximity between the faults, these high stresses can promote fault growth along strike if the initial spacing between the fault segments is large or can promote the formation of secondary oblique structures linking the main fault segments if the faults are close-spaced (e.g., Segall and Pollard, 1980; Bürgmann and Pollard, 1992, 1994; Nevitt et al., 2014; Nevitt, 2015).

Figs. 15 and 16 present data collected along two transects through the overlapping fault step models for convergence angles $30^\circ$ (Figs. 15a,b and 16a,b), $45^\circ$ (Figs. 15c,d and 16c,d) and $60^\circ$ (Figs. 15e,f and 16e,f). Transect 1 parallels faults through the center of the transpression zone while transect 2 orient perpendicular to the fault segments. The two transects record very different profiles

![Fig. 6. Maximum principal strain distribution for overlapping steps under convergence angle of a) 0°; b) 30°; c) 45°; d) 60°; and e) 90°.](image)

![Fig. 7. $\sigma_3$ (the minimum compressive stress) distribution for overlapping steps under convergence angle of 60° with the minimum values at the fault tips. Low-$\sigma_3$ zones develop in the tensional quadrants outside the contractional fault step.](image)
Fig. 8. Orientation of $\alpha_1$ for transpression zones within contractional fault step configurations with different combinations of overlap-to-separation ratio. a Underlapping steps; b Neutral steps; c Overlapping steps.

Fig. 9. Mean principal stress distribution for underlapping steps under convergence angle of a) 0°; b) 30°; c) 45°; d) 60°; and e) 90°.
of the principal stretch ($S_1$) and shear stress ($S_{12}$) magnitudes. Transect 2 demonstrates that in the direction orthogonal to the step-bounding faults, the stretch is focused into the step region, so that stretch difference increases with increasing convergence angle. On the other hand, transect 1 show that deformation decreases more gradually in the direction parallel to the faults.

4. Discussion

At the transpression zone, in addition to local uplift, contractional structures such as folds, thrust faults and pressure solution seams form on the contractional quadrant of the fault termination and often parallels the local $\sigma_3$ axis, in general. At the tips of mode II cracks or strike-slip faults, the local perturbation of the main stress field causes splay faults to occupy three distinct domains dominated respectively by shear, contractional, and extensional structures (Maerten et al., 2002, 2006; Goteti, 2009; Goteti and Mitra, 2013, 2016; Upton and Craw, 2016). Altering the strike of the fault segments relative to the direction of applied compressive stress (i.e., convergence angle) alters the geometry of linkage, because the symmetry of the system change. Oblique slip and convergence angles affect both the magnitude and the shape of the regions of stress concentration around the fault segments and within the transpression zone, showing changes in $z = 30^\circ$ to $60^\circ$ in comparison to $30^\circ$ to $60^\circ$. According to the maximum principle strain trajectories, before forming rhomboidal and sigmoidal transpression zones, secondary faults develop parallel to the fault segment displacement, but later parallel to the contractual step and accommodate an oblique-slip. The sigmoidal shape of the transpression zone in overlapping steps is due to increases in the amount of overlap, which results in a wider transpression zone and well-developed crosscutting faulting or internal faults (Westaway, 1995) linking the fault segments. These crosscutting faults are P-shear splay faults (see Misra and Mukherjee, in press-2 for field examples) or linkage that accommodates fault parallel shortening as shearing proceeds, and are outnumber R-shears (Keller et al., 1997; Schreurs and Colletta, 2002; Barreca and Maesano, 2012; Pennacchioni and Mancktelow, 2013). Furthermore, antithetic faults can develop in an en-échelon array (in the high angle $\sim 70^\circ$ to $90^\circ$ in neutral and underlapping steps and $\sim 30^\circ$ to $45^\circ$ for overlapping steps) along the high mean stress zones in between the fault segments (e.g. Kim et al., 2004; Barreca and Maesano, 2012; Pennacchioni and Mancktelow, 2013). Since 2D models presume faults to be vertical, this mean stress perturbation between fault segments is less in three-dimensional models. This is because the depth of faults is relatively short with respect to the model dimensions. More concentrated compressive stress on both sides of rhomboidal and the sigmoidal transpression zone can define a transpression zone with greater uplift in central areas (e.g. Upton et al., 2009) and make a doubly plunging anticlinal structure. These restricted sigmoidal zones to contractual fault steps appear like S-C ductile fabrics, mineral fishes, recrystallization and crystal-
plastic flow with a component of non-coaxial flow on the macroscopic-to-microscopic-scales (Lister and Snoke, 1984; Passchier and Trouw, 2005; Mukherjee, 2010b, 2011; Fossen, 2016). Under contractional condition in the fault steps, wing cracks and horsetail arrays development is restricted to $30^\circ \leq \alpha \leq 60^\circ$ (intermediate values of $\alpha$), whereas $S_1$ trajectories concentrate at the fault segment tips.

Fault interactions can give rise to a broad variety of local structures that can be explained in terms of the variations in the strain field predicted by the model. These results are consistent with recent field studies that point towards a complex deformation pattern in transpression zones within contractual fault steps. As the results show, three-dimensional stress/strain in the transpression zone with overstepping strike-slip systems typically involve rotation around a vertical axis. Rotational processes can be the attitude of this axis in natural prototype (such as thrust emplacement, local develop of oblique-slip faulting, and exhumed strike-slip systems) (e.g., Garfunkel and Ron, 1985; Channell et al., 1990; Oldow et al., 1990; Renda et al., 2000; Monaco and De Guidi, 2006; Avellone et al., 2010; Upton and Craw, 2014; Cao and Neubauer, 2016; Nabavi et al., 2016c). Stress/strain trajectories from underlapping steps to overlapping configuration reveal that transpression within contractual fault steps locally accommodate the regional stress field and may not be locked. Simultaneous simple shearing and pure shearing within transpression zone change the fault type and orientation when the boundary fault changes from pure strike-slip to oblique reverse-slip within the zone and generate an asymmetrical section across the zone, which symmetric geometries are only found in its central parts (e.g., Dooley et al., 1999; McClay and Bonora, 2001). Rotation of fault planes have already been simulated in models and ascertained in nature (review in Mukherjee, 2014a,b).

Various field studies on outcrop to regional scale transpression structures clearly reveal spatial and temporal variations in the extension directions with increasing contraction on the major faults. The broad variety in the orientations and kinematics of these local structures cannot be directly correlated to the deformation on the major faults and vice-versa. The maximum finite strains rotate towards the regional transport direction and transpression zone boundaries with progressive deformation. Therefore, local structures oblique to the major faults are common in incipient transpression zones. In subsequent stages of deformation, with increasing contraction on the faults, these local structures may be overprinted by younger generations of less oblique structures or, may be reactivate in conformance with the strain field (e.g., Ismat and Mitra, 2001). Numerical results suggest that even for an isotropic material, fault interactions result in non-coaxial strain paths and complex stress fields within transpression zones. The non-coaxiality of deformation in transpression zones (Nabavi et al., 2016b) has important implications for interpreting attendant structures and strain partitioning. Kinematics of oblique convergence and various related structures need to be cautiously

Fig. 11. Mean principal stress distribution for overlapping steps under convergence angle of a) $0^\circ$; b) $30^\circ$; c) $45^\circ$; d) $60^\circ$; and e) $90^\circ$. 
interpreted in terms of the 3D strain field, noting that the strains/stresses vary both temporally and spatially in the transpression zone. In fact, field studies in contractional settings, such as Zagros fold-and-thrust system (Sarkarinejad, 2007; Sarkarinejad and Azizi, 2008; Sarkarinejad et al., 2010, 2013) and Alborz Mountain Range (Ballato et al., 2013; Nabavi et al., 2016b, 2016c), clearly demonstrate that non-coaxial flow in rocks (Mukherjee et al., 2012; Mukherjee, 2013b) can result in a wide range of finite strain ellipsoid orientations corresponding to a single overall compressive stress regime. Note that the imposed maximum regional compressive stress in the present study is 80 MPa. In transpression zones characterized by higher convergence and contraction on the major fault steps, the non-coaxiality of the deformation will conceivably be significantly higher. Lithological and mechanical heterogeneities in natural transpression zone rocks further complicate the relationship between strains and stress.

4.1. Modelling the Esmail-abad — West Neh contractual fault step (Sistan Structural Zone, southeastern Iran)

4.1.1. Sistan Structural Zone

The Sistan Structural Zone (SSZ) in southeastern Iran a ∼N trending Cretaceous-Tertiary orogenic belt more than 700 km along the border area between Central Iran and Helmand (Afghan) blocks (Fig. 17a and b) (Tirrul et al., 1983; Walker and Jackson, 2004; Mohammadi et al., 2016). After the Afghan block rifted from the Lut block in Early Cretaceous, the SSZ formed by closing the north-south extension of the Neotethys Ocean (called the Sistan Ocean) between the Central Iranian Lut continental block and the Afghan microcontinent during Campanian to Paleocene times along an eastward dipping subduction zone (Camp and Griffis, 1982; Tirrul et al., 1983; Agard et al., 2011; Bröcker et al., 2013; Bayet-Goll et al., 2016; Mohammadi et al., 2016). The SSZ comprises three main sub-zones (Camp and Griffis, 1982; Tirrul et al., 1983; Perelló et al., 2008; Fotoohi-Rad et al., 2009; Saccani et al., 2010; Angiboust et al., 2013; Mohammadi et al., 2016) (Fig. 17b): 1) the Rutak Complex (the oldest part of SSZ) to the East, which consists of Cretaceous flysch, high-pressure, low-temperature metabasites, fault-bounded masses up to 15 km long ophiolitic units, and a metamorphic mélangé; 2) the Neh Complex as accretionary wedge to the West, which consists of late Cretaceous to Eocene flysch and some ophiolitic units; and 3) the Seidabeh Basin, which overlies the Rutak and Neh Complexes unconformably and consists of unmetamorphosed fore-arc sediments of Maastrichtian to Eocene age. The SSZ contains various backthrust and active sub-parallel strike-slip faults as en-échelon arrays that formed many extensional (releasing) and contractual (restraining) steps/bends along the faults. Generally, the deformation in eastern Iran is controlled by the right-lateral strike-slip that is north-south to northwest-southeast trending (Berberian et al., 2000; Walker and Jackson, 2004; Parsons et al., 2006; Mohammadi et al., 2016).
4.1.2. Esmail-abad — West Neh contractual fault step

The Esmail-abad right-lateral strike-slip fault with a reverse-slip component is one of the segments of the Nehbandan continental basement fault, which is the structural boundary between the SSZ and the Lut block structural zones (Fig. 17c and d). It extends as ~ N trending ~70 km long fault between the Sah-abad and Nehbandan areas (Walker and Khatib, 2006). The West Neh fault is one of the right-lateral strike-slip segments of the Neh fault system and also trends N. These two fault segments form a left-stepping geometry and create a contractual step (Fig. 17c and d). According to the Iranian Permanent Global Positioning System Network (IPGN) (www.ipgn.ncc.org.ir) the velocity of eastern Iran is 8 mm/yr and the local compressive stress directs N26°E. Hence, a transpression zone, named Kuh-e-Hori, between the two fault segments has formed at an altitude of ~2700 m (Fig. 17c). At the surface, this transpression zone comprises shale, sandstone, and limestone lenses (partly metamorphosed) (Paleogene) with ultrabasic, volcanic rocks (Neogene). Quaternary terraces and alluvial fans are outside this zone. The Kuh-e-Hori transpression zone has a central rhomboidal shape, is bounded by two outer steep reverse faults, and its maximum uplift is located in the center of the fault step. Given the far-field compressive stress direction of N26°E and the transpression zone characteristics, the fault segments indicate a neutral step geometry (i.e., 90° restraining step). The structural features of Kuh-e-Hori correlates well with our FE-results in the neutral step geometry at far-field compressive stress direction of N30°E (Fig. 18a–d). The circular pattern of the maximum principal stress trajectories, deduced by means of McClay and Bonora (2001) and Dooley and Schreurs (2012), is located much more around the fault tips than within the transpression zone, which is dominated with highlands (i.e., Kuh-e-Hori). Also, the maximum principal strain trajectories concentrate within the transpression zone along a NW-SE direction that developed contractual structures such as folds and reverse faults. The results show the capability of fault segments in the transpression zone to increase the mean principal stress during all simulated stages of the transpression zone. The mean stress pattern can be characterized as having greater magnitude within transpression zone than at the fault tips and outside the zone (as Sahl-abad subsidence) (Figs. 17c and 18c). The maximum stress concentration in the central part of the zone shows the relative motions of the advancing sides of the two fault segments, which are opposed in the zone and control the mean stress concentration (Fig. 18b). Six topographic sections across the Kuh-e-Hori (AA’–FF’) (Fig. 17d and e) shows a moderate, yet distinct asymmetry and maximum uplift in the central part of the zone (as per Dooley et al., 1999; McClay and Bonora, 2001; Dooley and Schreurs, 2012 analogue models). The asymmetrical uplift in response to obliquely applied stress loading is controlled by the finite fault length. The asymmetric transpression zone is bounded by moderately dipping, and oblique reverse faults. Asymmetric geometries decrease in the central parts. In addition, serial sections (from AA’-EE’) (Fig. 17e) show that the Kuh-e-Hori transpression...
zone is formed as a doubly plunging anticline.

5. Conclusions

Stress distribution and strain localization patterns were obtained for a set of 2D FE-models of a transpression zone related to two pre-existing right-stepping left-lateral strike-slip fault segments as a function of the remotely applied compressive stress. Linear elastic rheology and plain strain conditions were assumed. In each simulation, different convergence angles $\alpha$, 0° (pure strike-slip), 30°, 45°, 60° and 90° (pure contraction) were applied to the three representative end-member fault segment interaction models, which were underlapping, neutral, and overlapping contractional steps. The numerical results indicate that the displacement vectors are oblique to the regional transport direction throughout the deformation history. With increasing contraction, the magnitude of displacement within the transpression zone increases. Orientations of the $\sigma_1$ and $\sigma_3$ orientations strongly depend on the structural position within the transpression zone. In low-$\sigma_3$ (the minimum compressive stress) zones, which are concentrated around fault tips, wing cracks and horsetail arrays would therefore develop outwards along a curvilinear path. For overlapping fault steps, the $\sigma_1$ (the maximum compressive stress) orientations within the transpression zone are highly deflected and rotate to become parallel with the zone bounding strike-slip faults. This pattern was created by two clockwise flow rotations around the fault tips due to friction effect and different shear components, from pure shear outside of the fault steps toward simple shear along the fault segments. This causes the perturbed stress field which reflects the heterogeneous nature of deformation. Lozenge-shaped transpression zones are characterize the underlapping steps, whereas rhomboidal and strongly sigmoidal transpression zones are characteristics of neutral and overlapping steps, respectively. Transpression zones are affected by curved, synthetic and antithetic oblique-slip reverse faults that cause block rotation between segments and show the asymmetric geometries in the section. Symmetric geometries are only found in the central parts of the zone. Within overlapping fault steps, crosscutting faults transect the central parts of the transpression zone as hard-linkage and the clear contractional linking damage zone. The mean stress pattern is similar to the pattern in contractional steps and decreases and increases, respectively, from underlapping configuration toward overlapping fault steps. Two pairs of local minimum (at the extensional quadrant of the tips) and maximum (at the compressional quadrant of the tips) mean stress patterns developed at the tips of the fault segments. In general, mechanical interaction between the fault segments decreases with increasing the overlap-to-separation ratio. Oblique slip and convergence angles affect both the magnitude and the shape of the regions of stress concentration around fault segments and within the transpression zone, so that models show the changes in $\alpha = 30°-60°$ compared with $30°<\alpha$ and $60°<\alpha$. The natural example of the Kuh-e-Hori...
Fig. 15. Model results of maximum principal stretch ($S_1$) for overlapping steps in convergence angles $30^\circ$ (a,b), $45^\circ$ (c,d) and $60^\circ$ (e,f). Left and right columns show transect 1 and transect 2, respectively.
Fig. 16. Model results of shear stress ($S_{12}$) for overlapping steps in convergence angles 30° (a,b), 45° (c,d) and 60° (e,f). Left and right columns show transect 1 and transect 2, respectively.
Fig. 17. a Regional overview of Iran; b Simplified geological map of the northern part of the Sistan Suture Zone (after Fotoohi-Rad et al., 2009; Bröcker et al., 2013; Bayet-Goll et al., 2016). c Google Earth™ image of the Kuh-e-Hori transpression zone from the map view. d Digital elevation model with simplified structural map of the Kuh-e-Hori transpression zone between the Esmail-abad and West Neh left-stepping right-lateral strike-slip fault segments. e Serial topographic sections across the Kuh-e-Hori transpression zone. Sections are named in accordance with (Fig. 16d).
transpression zone between the two left-stepping right-lateral strike-slip fault segments of Esmail-abad and West Neh, SE Iran, shows comparable structural and geomorphological geometries to the neutral step configuration.

Acknowledgements

We would like to express our thanks to Dr. Frantz Maerten for very detailed and constructive reviews and comments that improved the manuscript. This work forms part of the Ph.D. thesis of Seyed Tohid Nabavi at Shahid Beheshti University, Tehran. We thank reviewers Soumyajit Mukherjee and Phaedra Upton for their attentive reading and constructive comments that improved the manuscript. Also, editorial and handling work by Ian Alsop is gratefully acknowledged.

References


Fig. 18. Model results of a maximum principal strain, b maximum principal stress, c mean principal stress, and d minimum principal stress distribution for Kuh-e-Hori transpression zone.


Mukherjee, S., 2010a. Structures in meso- and micro-scale in the sutlej section of the higher himalayan shear zone, Indian Himalaya. e-Terra 7, 1–27.


Mukherjee, S., 2013a. Structures in meso- and micro-scale in the sutlej section of the higher himalayan shear zone, Indian Himalaya. e-Terra 7, 1–27.


localization mechanisms in a 3-D fractured medium under rotating compressive stress orientations. Tectonophysics 593, 95–110.


